

#31 $\frac{(x+3)(x+1)}{3}$

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In Exercises 23–34, simplify the complex fraction.

23. $\frac{\left(\frac{x}{3} - 4\right)}{\left(5 + \frac{1}{x}\right)} = \frac{x(x-12)}{3(5x-1)}$

24. $\frac{\left(\frac{4}{x} + 2\right)}{\left(\frac{1}{2x} - 8\right)} = \frac{4(2+x)}{(1-16x)}$

25. $\frac{\left(\frac{3}{x^2} + \frac{1}{x}\right)}{\left(2 - \frac{4}{5x}\right)} = \frac{(5x+3)}{2x(5x-2)}$

26. $\frac{\left(16 - \frac{1}{x^2}\right)}{\left(\frac{1}{4x^2} - 4\right)} = -4$

27. $\frac{\left(\frac{10}{x+1}\right)}{\left(\frac{1}{2} + \frac{3}{x+1}\right)} = \frac{20}{x+7}$

28. $\frac{\left(\frac{2}{3x+15}\right)}{\left(\frac{2}{x+5} + \frac{1}{4x+20}\right)} = \frac{8}{27}$

29. $\frac{\left(\frac{1}{2x+1} - \frac{3}{4(2x+1)}\right)}{\left(\frac{x}{2x+1}\right)} = \frac{1}{4x}$

30. $\frac{\left(\frac{2}{x^2-1} + \frac{1}{x+1}\right)}{\left(\frac{1}{12x^2-3}\right)} = \frac{3(4x^2-1)}{(x-1)}$

31. $\frac{\left(\frac{1}{x+1} + \frac{1}{2}\right)}{\left(\frac{3}{2x^2+4x+2}\right)}$

32. $\frac{\left(\frac{x}{x-3} - \frac{2}{3}\right)}{\left(\frac{10}{3x} + \frac{x^2}{x-3}\right)} = \frac{x(x+6)}{(3x^3+10x-30)}$

33. $\frac{\left(\frac{1}{2x} - \frac{6}{x+5}\right)}{\left(\frac{x}{x-5} + \frac{1}{x}\right)} = \frac{(11x+5)(x-5)}{2(x+5)(x^2-x-5)}$

34. $\frac{\left(\frac{4}{x^2-9} + \frac{2}{x-3}\right)}{\left(\frac{1}{x+3} + \frac{1}{x-3}\right)} = \frac{(x+5)}{x}$

In Exercises 35–40, solve the equation.

35. $\frac{\left(\frac{4}{x} + \frac{6}{x+1}\right)}{\left(\frac{3}{x+1} - 5\right)} = -1$
 $x = 2$

36. $\frac{\left(\frac{3}{x-2} + 2\right)}{\left(\frac{2x-3}{x-2} + \frac{2x}{3}\right)} = 1$
 $x = 3, 1$

37. $\frac{\left(x - \frac{5x+3}{x-1}\right)}{\left(\frac{2x}{2x-2} - \frac{x}{2}\right)} = -2$
 $x = -1$

38. $\frac{\left(\frac{3x}{x-1} - \frac{4}{x}\right)}{\left(\frac{1}{2x} - \frac{1}{x}\right)} = 16$
 $x = \frac{2}{3}, -2$

39. $\frac{\left(\frac{x}{x-2} + \frac{7}{x}\right)}{\left(6 - \frac{12}{x}\right)} = -1$
 $x = \frac{10}{7}, 1$

40. $\frac{\left(\frac{x+4}{5} - 3\right)}{\left(\frac{1}{2} + \frac{x+4}{10}\right)} = -2$
 $x = 1$

Doctors In Exercises 41 and 42, use the following information.

For 1970 to 1990, the number of doctors of medicine, M (in thousands), in the United States can be approximated by

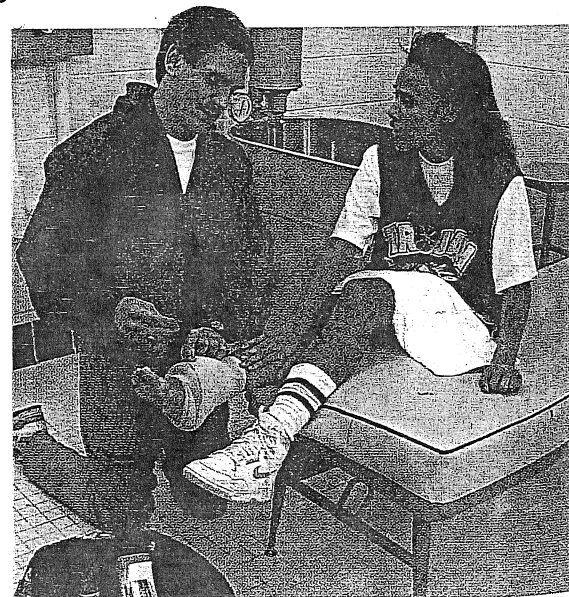
$$M = \frac{28,390 + 693t}{85 - t},$$

where $t = 0$ represents 1970. The number of doctors of osteopathy, B (in thousands), can be approximated by

$$B = \frac{776 - 12t}{55 - 2t}.$$

41. Write an expression for the total number, I , of doctors of medicine (MD) and doctors of osteopathy (DO). Simplify the result.

42. How many MDs and DOs did the United States have in 1985?



$\approx 554,000, \approx 24,000$

41 $I = \frac{-1374t^2 - 20,461t + 1,629,410}{(85-t)(55-2t)}$